

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and
Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

Verification and Validation of Simulation Models

Impressive slide presentations

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Purpose and Overview

- ▶ The goal of the validation process is:
 - ▶ To produce a model that represents true behavior closely enough for decision-making purposes
 - ▶ To increase the model's credibility to an acceptable level
- ▶ Validation is an integral part of model development:
 - ▶ Verification: building the model correctly, correctly implemented with good input and structure
 - ▶ Validation: building the correct model, an accurate representation of the real system
- ▶ Most methods are informal subjective comparisons while a few are formal statistical procedures

Validation

Purpose and Overview

Modeling-Building,
Verification and
Validation

Verification

Examination of Model
Output

Other Important
Tools

Calibration and Validation

Calibration and
Validation

Face Validity

Validate Model
Assumptions

Validate Input-Output
Transformation

Bank Example

Comparison with Real
System Data

Hypothesis Testing

Type II Error

Confidence Interval
Testing

Using Historical Input
Data

Using a Turing Test

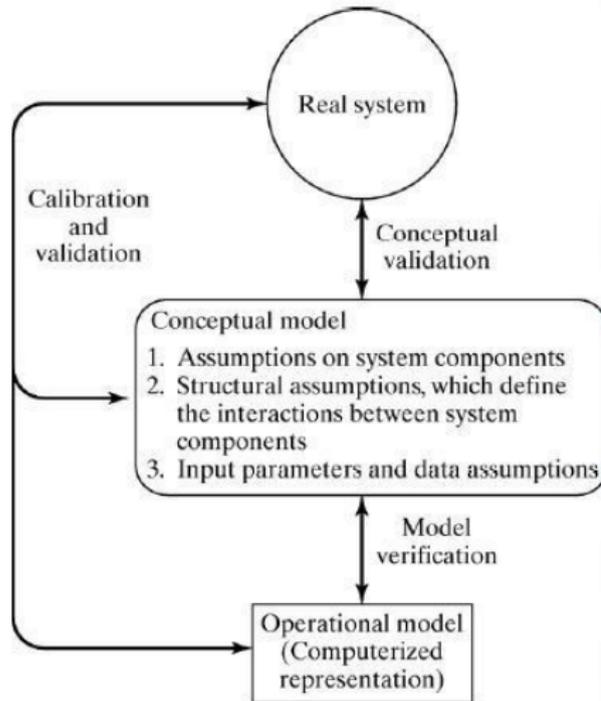
Summary

References

Modeling-Building, Verification and Validation

Steps in Model-Building

- ▶ Observing the real system and the interactions among their various components and of collecting data on their behavior.
- ▶ Construction of a conceptual model
- ▶ Implementation of an operational model



Validation

Purpose and Overview

**Modeling-Building,
Verification and
Validation**

Verification

Examination of Model
Output

Other Important
Tools

Calibration and Validation

Calibration and
Validation

Face Validity

Validate Model
Assumptions

Validate Input-Output
Transformation

Bank Example

Comparison with Real
System Data

Hypothesis Testing

Type II Error

Confidence Interval
Testing

Using Historical Input
Data

Using a Turing Test

Summary

References

- ▶ Purpose: ensure the conceptual model is reflected accurately in the computerized representation.
- ▶ Many common-sense suggestions, for example:
 - ▶ Have someone else check the model.
 - ▶ Make a flow diagram that includes each logically possible action a system can take when an event occurs.
 - ▶ Closely examine the model output for reasonableness under a variety of input parameter settings.
 - ▶ Print the input parameters at the end of the simulation, make sure they have not been changed inadvertently.
 - ▶ Make the operational model as self-documenting as possible.
 - ▶ If the operational model is animated, verify that what is seen in the animation imitates the actual system.
 - ▶ Use the debugger.
 - ▶ If possible use a graphical representation of the model.

Validation

Purpose and Overview

Modeling-Building,
Verification and
Validation

Verification

Examination of Model
Output

Other Important
Tools

Calibration and Validation

Calibration and
Validation

Face Validity

Validate Model
Assumptions

Validate Input-Output
Transformation

Bank Example

Comparison with Real
System Data

Hypothesis Testing

Type II Error

Confidence Interval
Testing

Using Historical Input
Data

Using a Turing Test

Summary

References

Examination of Model Output for Reasonableness I

- ▶ Two statistics that give a quick indication of model reasonableness are *current contents* and *total counts*
 - ▶ **Current content:** The number of items in each component of the system at a given time.
 - ▶ **Total counts:** Total number of items that have entered each component of the system by a given time.
- ▶ Compute certain long-run measures of performance, e.g. compute the long-run server utilization and compare to simulation results.
- ▶ A model of a complex network of queues consisting of many service centers.
 - ▶ If the current content grows in a more or less linear fashion as the simulation run time increases, it is likely that a queue is unstable

Validation

Purpose and Overview

Modeling-Building,
Verification and
Validation

Verification

Examination of Model
Output

Other Important
Tools

Calibration and Validation

Calibration and
Validation

Face Validity

Validate Model
Assumptions

Validate Input-Output
Transformation

Bank Example

Comparison with Real
System Data

Hypothesis Testing

Type II Error

Confidence Interval
Testing

Using Historical Input
Data

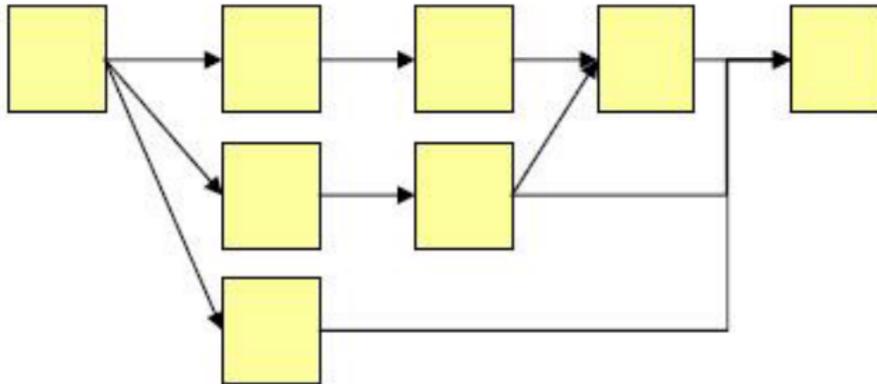
Using a Turing Test

Summary

References

Examination of Model Output for Reasonableness II

- ▶ If the total count for some subsystem is zero, indicates no items entered that subsystem, a highly suspect occurrence
- ▶ If the total and current count are equal to one, can indicate that an entity has captured a resource but never freed that resource.



Validation

Purpose and Overview

Modeling-Building,
Verification and
Validation

Verification

**Examination of Model
Output**

Other Important
Tools

Calibration and Validation

Calibration and
Validation

Face Validity

Validate Model
Assumptions

Validate Input-Output
Transformation

Bank Example

Comparison with Real
System Data

Hypothesis Testing

Type II Error

Confidence Interval
Testing

Using Historical Input
Data

Using a Turing Test

Summary

References

Other Important Tools

- ▶ Documentation
 - ▶ A means of clarifying the logic of a model and verifying its completeness.
 - ▶ Comment the operational model, definition of all variables and parameters.
- ▶ Use of a trace
 - ▶ A detailed printout of the state of the simulation model over time.
 - ▶ Can be very labor intensive if the programming language does not support statistic collection.
 - ▶ Labor can be reduced by a centralized tracing mechanism
 - ▶ In object-oriented simulation framework, trace support can be integrated into class hierarchy. New classes need only to add little for the trace support.

Validation

Purpose and Overview

Modeling-Building,
Verification and
Validation

Verification

Examination of Model
Output

**Other Important
Tools**

Calibration and Validation

Calibration and
Validation

Face Validity

Validate Model
Assumptions

Validate Input-Output
Transformation

Bank Example

Comparison with Real
System Data

Hypothesis Testing

Type II Error

Confidence Interval
Testing

Using Historical Input
Data

Using a Turing Test

Summary

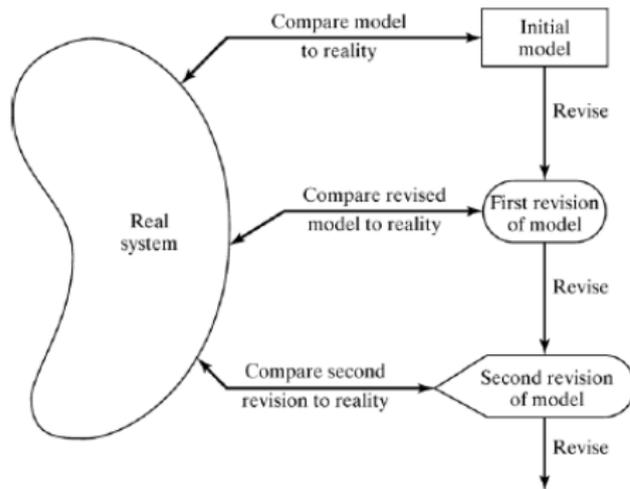
References

Calibration and Validation

- ▶ Validation: the overall process of comparing the model and its behavior to the real system.
- ▶ Calibration: the iterative process of comparing the model to the real system and making adjustments.

Comparison of the model to real system

- ▶ Subjective tests
 - ▶ People who are knowledgeable about the system
- ▶ Objective tests
 - ▶ Requires data on the real system's behavior and the output of the model



Validation

- Purpose and Overview
- Modeling-Building, Verification and Validation
- Verification
- Examination of Model Output
- Other Important Tools

Calibration and Validation

- Calibration and Validation
- Face Validity
- Validate Model Assumptions
- Validate Input-Output Transformation
- Bank Example
- Comparison with Real System Data
- Hypothesis Testing
- Type II Error
- Confidence Interval Testing
- Using Historical Input Data
- Using a Turing Test

Summary

References

- ▶ Danger during the calibration phase
 - ▶ Typically few data sets are available, in the worst case only one, and the model is only validated for these.
 - ▶ Solution: If possible collect new data sets
- ▶ No model is ever a perfect representation of the system
 - ▶ The modeler must weigh the possible, but not guaranteed, increase in model accuracy versus the cost of increased validation effort.
- ▶ Three-step approach for validation:
 1. Build a model that has high face validity.
 2. Validate model assumptions.
 3. Compare the model input-output transformations with the real system's data.

Validation

Purpose and Overview

Modeling-Building,
Verification and
Validation

Verification

Examination of Model
Output

Other Important
Tools

Calibration and Validation

Calibration and
Validation

Face Validity

Validate Model
Assumptions

Validate Input-Output
Transformation

Bank Example

Comparison with Real
System Data

Hypothesis Testing

Type II Error

Confidence Interval
Testing

Using Historical Input
Data

Using a Turing Test

Summary

References

High Face Validity

- ▶ Ensure a high degree of realism:
 - ▶ Potential users should be involved in model construction from its conceptualization to its implementation.
- ▶ Sensitivity analysis can also be used to check a model's face validity.
 - ▶ Example: In most queueing systems, if the arrival rate of customers were to increase, it would be expected that server utilization, queue length and delays would tend to increase.
 - ▶ For large-scale simulation models, there are many input variables and thus possibly many sensitivity tests.
 - ▶ Sometimes not possible to perform all of these tests, select the most critical ones.

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

Validate Model Assumptions

- ▶ General classes of model assumptions:
 - ▶ Structural assumptions: how the system operates.
 - ▶ Data assumptions: reliability of data and its statistical analysis.
- ▶ Bank example: customer queueing and service facility in a bank.
 - ▶ Structural assumptions
 - ▶ Customer waiting in one line versus many lines
 - ▶ Customers are served according FCFS versus priority
 - ▶ Data assumptions, e.g., interarrival time of customers, service times for commercial accounts.
 - ▶ Verify data reliability with bank managers
 - ▶ Test correlation and goodness of fit for data

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

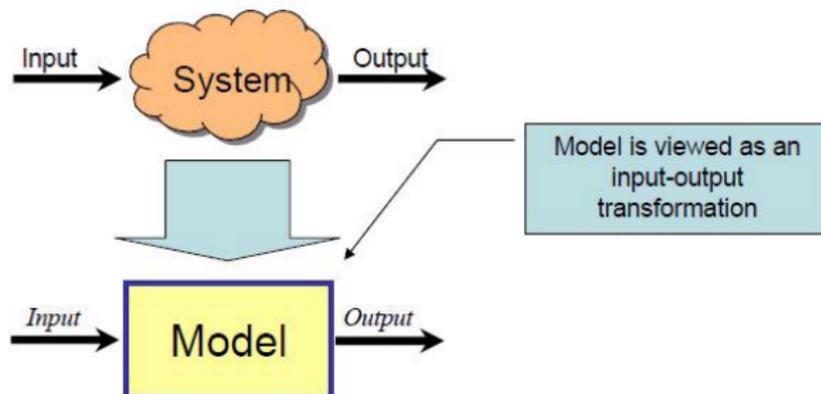
Calibration and
Validation
Face Validity
**Validate Model
Assumptions**
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

Validate Input-Output Transformation

- ▶ Goal: Validate the model's ability to predict future behavior
 - ▶ The only objective test of the model.
 - ▶ The structure of the model should be accurate enough to make good predictions for the range of input data sets of interest.
- ▶ One possible approach: use historical data that have been reserved for validation purposes only.
- ▶ Criteria: use the main responses of interest.



Bank Example

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

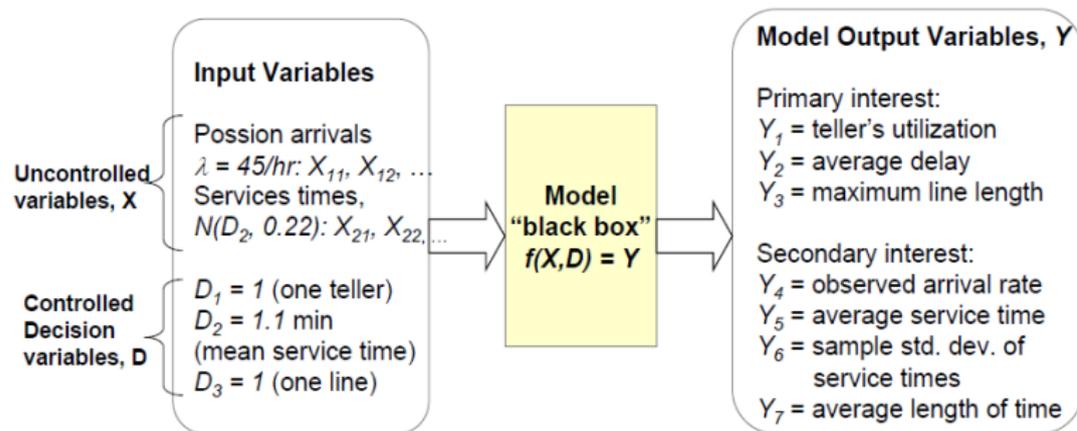
References

- ▶ Example: One drive-in window serviced by one teller, only one or two transactions are allowed.
 - ▶ Data collection: 90 customers during 11 am to 1 pm.
 - ▶ Observed service times $\{S_i, i = 1, 2, \dots, 90\}$.
 - ▶ Observed interarrival times $\{A_i, i = 1, 2, \dots, 90\}$.
 - ▶ Data analysis led to the conclusion that:
 - Interarrival times: exp. distr. with rate $\lambda = 45$
 - Service times: $N(1.1, 0.22^2)$

Input vars

Bank Example – The Black Box

- ▶ A model was developed in close consultation with bank management and employees
- ▶ Model assumptions were validated
- ▶ Resulting model is now viewed as a “black box”:



Validation

- Purpose and Overview
- Modeling-Building, Verification and Validation
- Verification
- Examination of Model Output
- Other Important Tools

Calibration and Validation

- Calibration and Validation
- Face Validity
- Validate Model Assumptions
- Validate Input-Output Transformation
- Bank Example**
- Comparison with Real System Data
- Hypothesis Testing
- Type II Error
- Confidence Interval Testing
- Using Historical Input Data
- Using a Turing Test

Summary

References

Comparison with Real System Data

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
**Comparison with Real
System Data**
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

- ▶ Real system data are necessary for validation.
 - ▶ System responses should have been collected during the same time period (from 11am to 1pm on the same day.)
- ▶ Compare the average delay from the model Y_2 with the actual delay Z_2 :
 - ▶ Average delay observed, $Z_2 = 4.3$ minutes, consider this to be the true mean value $\mu_0 = 4.3$.
 - ▶ When the model is run with generated random variates X_{1n} and X_{2n} , Y_2 should be close to Z_2 .

Comparison with Real System Data

- ▶ Six statistically independent replications of the model, each of 2-hour duration, are run.

Replication	Y_4 Arrivals/Hour	Y_5 Service Time [Minutes]	Y_2 Average Delay [Minutes]
1	51	1.07	2.79
2	40	1.12	1.12
3	45.5	1.06	2.24
4	50.5	1.10	3.45
5	53	1.09	3.13
6	49	1.07	2.38
Sample mean			2.51
Standard deviation			0.82

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

Hypothesis Testing I

- ▶ Compare the average delay from the model Y_2 with the actual delay Z_2
- ▶ Null hypothesis testing: evaluate whether the simulation and the real system are the same (w.r.t. output measures):

$$H_0 : E(Y_2) = 4.3 \text{ min}$$

$$H_1 : E(Y_2) \neq 4.3 \text{ min}$$

- ▶ If H_0 is not rejected, then, there is no reason to consider the model invalid
- ▶ If H_0 is rejected, the current version of the model is rejected, and the modeler needs to improve the model
- ▶ **Conduct the t test:**
- ▶ Chose level of significance ($\alpha = 0.5$) and sample size ($n = 6$).

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

Hypothesis Testing II

- ▶ Compute the same mean and sample standard deviation over the n replications:

$$\bar{Y}_2 = \frac{1}{n} \sum_{i=1}^n Y_{2i} = 2.51 \text{ min} \quad S = \sqrt{\frac{\sum_{i=1}^n (Y_{2i} - \bar{Y}_2)^2}{n-1}}$$

- ▶ Compute test statistics (two-sided test):

$$|t_0| = \left| \frac{Y_2 - \mu_0}{\frac{S}{\sqrt{n}}} \right| = \left| \frac{2.51 - 4.3}{0.82\sqrt{6}} \right| = 5.36 > t_{crit} = 2.571$$

- ▶ Hence, reject H_0 . Conclude that the model is inadequate.
- ▶ Check: the assumptions justifying a t test, that the observations (Y_{2i}) are normally and independently distributed.

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

Hypothesis Testing III

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data

Hypothesis Testing

Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

- ▶ Similarly, compare the model output with the observed output for other measures: $Y_4 \leftrightarrow Z_4$, $Y_5 \leftrightarrow Z_5$, and $Y_6 \leftrightarrow Z_6$

Type II Error I

- ▶ For validation, the power of the test is:
 - ▶ Probability[detecting an invalid model] = $1 - \beta$
 - ▶ $\beta = P(\text{Type II error}) = P(\text{failing to reject } H_0 | H_1 \text{ is true})$
 - ▶ Consider failure to reject H_0 as a strong conclusion, the modeler would want β to be small.
 - ▶ Value of β depends on:
 - ▶ Sample size, n
 - ▶ The true difference, δ , between $E(Y)$ and μ :

$$\delta = \frac{|E(Y) - \mu|}{\sigma}$$

- ▶ In general, the best approach to control β error is:
 - ▶ Specify the critical difference, δ .
 - ▶ Choose a sample size, n , by making use of the operating characteristics curve (OC curve).

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

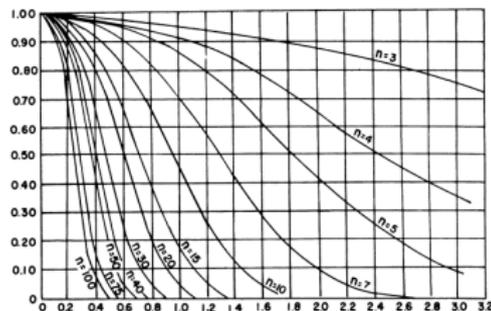
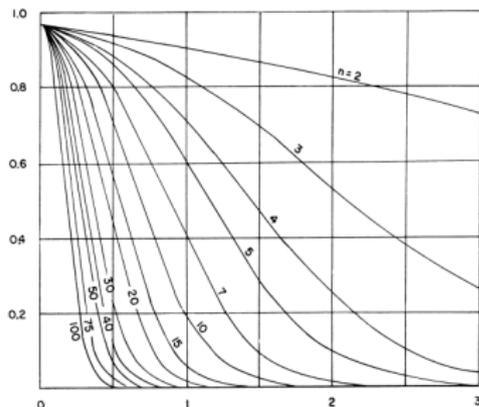
Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

Type II Error II

- ▶ Operating characteristics curve (OC curve) is the graph of the probability of a type II error $\beta(\delta)$ versus δ for a given sample size n



Validation

- Purpose and Overview
- Modeling-Building, Verification and Validation
- Verification
- Examination of Model Output
- Other Important Tools

Calibration and Validation

- Calibration and Validation
- Face Validity
- Validate Model Assumptions
- Validate Input-Output Transformation
- Bank Example
- Comparison with Real System Data
- Hypothesis Testing
- Type II Error**
- Confidence Interval Testing
- Using Historical Input Data
- Using a Turing Test

Summary

References

Type I and II Error

- ▶ Type I error (α):
 - ▶ Error of rejecting a valid model.
 - ▶ Controlled by specifying a small level of significance α .
- ▶ Type II error (β):
 - ▶ Error of accepting a model as valid when it is invalid.
 - ▶ Controlled by specifying critical difference and find the n .
- ▶ For a fixed sample size n , increasing α will decrease β .

Statistical Terminology	Modeling Terminology	Associated Risk
Type I: rejecting H_0 when H_0 is true	Rejecting a valid model	α
Type II: failure to reject H_0 when H_1 is true	Failure to reject an invalid model	β

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

Confidence Interval Testing I

- ▶ Confidence interval testing: evaluate whether the simulation and the real system performance measures are close enough.
- ▶ If Y is the simulation output, and $\mu = E(Y)$
- ▶ The confidence interval (CI) for μ is:

$$\bar{Y} \pm t_{\alpha/2, n-1} \frac{S}{\sqrt{n}}$$

- ▶ Validating the model - ε is a difference value chosen by the analyst, that is small enough to allow valid decisions to be based on simulations:
 - ▶ Suppose the CI does not contain μ_0 :
 - ▶ If the best-case error is $> \varepsilon$, model needs to be refined.
 - ▶ If the worst-case error is $\leq \varepsilon$, accept the model.
 - ▶ If best-case error is $\leq \varepsilon$, additional replications are necessary.

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

Confidence Interval Testing – Bank example

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
**Confidence Interval
Testing**
Using Historical Input
Data
Using a Turing Test

Summary

References

- ▶ $\mu_0 = 4.3$, and “close enough” is $\varepsilon = 1$ minute of expected customer delay.
- ▶ A 95% confidence interval, based on the 6 replications is [1.65, 3.37] because:

$$\bar{Y} \pm t_{0.025,5} \frac{S}{\sqrt{n}} = 2.51 \pm 2.571 \cdot \frac{0.82}{\sqrt{6}}$$

- ▶ $\mu_0 = 4.3$ falls outside the confidence interval,
 - ▶ the best case $|3.37 - 4.3| = 0.93 < 1$, but
 - ▶ - the worst case $|1.65 - 4.3| = 2.65 > 1$
 - ▶ **Additional replications are needed to reach a decision.**

Using Historical Input Data

Validation

Purpose and Overview

Modeling-Building,
Verification and
Validation

Verification

Examination of Model
Output

Other Important
Tools

Calibration and Validation

Calibration and
Validation

Face Validity

Validate Model
Assumptions

Validate Input-Output
Transformation

Bank Example

Comparison with Real
System Data

Hypothesis Testing

Type II Error

Confidence Interval
Testing

**Using Historical Input
Data**

Using a Turing Test

Summary

References

- ▶ An alternative to generating input data:
 - ▶ Use the actual historical record.
 - ▶ Drive the simulation model with the historical record and then compare model output to system data.
 - ▶ In the bank example, use the recorded interarrival and service times for the customers

$$\{(A_n, S_n), n = 1, 2, \dots\}$$

- ▶ Procedure and validation process: similar to the approach used for system generated input data.

Using a Turing Test I

- ▶ Use in addition to statistical test, or when no statistical test is readily applicable.
- ▶ **Turing Test**
 - ▶ *Described by Alan Turing in 1950. A human judge is involved in a natural language conversation with a human and a machine. If the judge cannot reliably tell which of the partners is the machine, then the machine has passed the test.*
- ▶ Utilize persons' knowledge about the system.
- ▶ For example:
 - ▶ Present 10 system performance reports to a manager of the system.
- ▶ Five of them are from the real system and the rest are “fake” reports based on simulation output data.

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

Using a Turing Test II

- ▶ If the person identifies a substantial number of the fake reports, interview the person to get information for model improvement.
- ▶ If the person cannot distinguish between fake and real reports with consistency, conclude that the test gives no evidence of model inadequacy.

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data

Using a Turing Test

Summary

References

Summary

- ▶ Model validation is essential:
 - ▶ Model verification
 - ▶ Calibration and validation
 - ▶ Conceptual validation
- ▶ Best to compare system data to model data, and make comparison using a wide variety of techniques.
- ▶ Some techniques that we covered:
 - ▶ Insure high face validity by consulting knowledgeable persons.
 - ▶ Conduct simple statistical tests on assumed distributional forms.
 - ▶ Conduct a Turing test.
 - ▶ Compare model output to system output by statistical tests.

Validation

Purpose and Overview
Modeling-Building,
Verification and
Validation
Verification
Examination of Model
Output
Other Important
Tools

Calibration and Validation

Calibration and
Validation
Face Validity
Validate Model
Assumptions
Validate Input-Output
Transformation
Bank Example
Comparison with Real
System Data
Hypothesis Testing
Type II Error
Confidence Interval
Testing
Using Historical Input
Data
Using a Turing Test

Summary

References

References

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Validation

- Purpose and Overview
- Modeling-Building, Verification and Validation
- Verification
- Examination of Model Output
- Other Important Tools

Calibration and Validation

- Calibration and Validation
- Face Validity
- Validate Model Assumptions
- Validate Input-Output Transformation
- Bank Example
- Comparison with Real System Data
- Hypothesis Testing
- Type II Error
- Confidence Interval Testing
- Using Historical Input Data
- Using a Turing Test

Summary

References