

DISCUSSION OF HYBRID JS-CONTRACTIONS IN b -METRIC SPACES WITH APPLICATIONS TO THE EXISTENCE OF SOLUTIONS FOR INTEGRAL EQUATIONS

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Abstract. The purpose of this work is to introduce the new concept of a hybrid JS-contraction in b -metric spaces which includes various contractions in such spaces. The existence and uniqueness of a fixed point for self mappings satisfying the proposed contractive condition on b -metric spaces are studied. As an application, the existence result of a unique solution for integral equations is also given in order to illustrate the effectiveness of the obtained results.

Key Words and Phrases: Hybrid JS-contractions, b -metric spaces, integral equations.

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