

## GEOMETRICAL PROPERTIES OF $l_p$ SPACES

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**Abstract.** In this work, some geometrical properties of Hilbert spaces are investigated in  $l_p$  spaces, for  $p \geq 2$ . As an application, we obtain an extension of the Banach Contraction Principle for best proximity points. The case of nonexpansive mappings is also discussed.

**Key Words and Phrases:** Best proximity points, fixed points,  $l_p$  spaces, P-property, contraction mappings, nonexpansive mappings, uniformly convex, strictly convex reflexive, proximal sets.

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