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MATHEMATICA

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MATHEMATICA was founded by Petre Sergescu in 1929 with the support of Dimitrie Pompeiu and Gheorghe Țițeica (the first directors of the journal), as well as of other members of the Faculty of Sciences from the University of Cluj. The journal was published without interruption between 1929 and 1948 and then, as a new series, from 1959 until today.

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