

WEAK OPENNESS AND WEAK CONTINUITY
IN IDEAL TOPOLOGICAL SPACES

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Abstract. Our purpose is to introduce the concepts of weakly \star -open functions and weakly \star -continuous functions. Moreover, some characterizations of weakly \star -continuous functions and $\theta(\star)$ -continuous functions are investigated. In particular, the relationships between weakly \star -continuous functions and $\theta(\star)$ -continuous functions are established.

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