

LEAST PRIMES WHICH SPLIT IN IMAGINARY
QUADRATIC FIELDS

SAKHA A. ALKABOUSS, BOUALEM BENSEBA, OMAR KIHHEL, and JESSE LARONE

Abstract. In this paper, we bound the least primes which split in an imaginary quadratic field in terms of its class number.

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Université Cheikh Anta Diop
Département de Mathématiques
Sénégal
E-mail: sakha.alkabouss@ucad.edu.sn

Université des Sciences et de
la Technologie Houari Boumediene
Faculté de Mathématiques
Algiers, Algeria
E-mail: b.benseba@usthb.dz

Brock University
Department of Mathematics and Statistics
St. Catharines, Canada
E-mail: okihel@brocku.ca
E-mail: jlarone@brocku.ca