

STRONG REGULARITY OF SMASH PRODUCTS
ASSOCIATED WITH G -SET GRADINGS

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Abstract. For a group G , a G -graded ring R and a finite left G -set A , we study the strong regularity of the smash product $R\#A$.

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