

## SOME PERTURBED INEQUALITIES OF OSTROWSKI TYPE FOR TWICE DIFFERENTIABLE FUNCTIONS

SAMET ERDEN, HÜSEYİN BUDAK, and MEHMET ZEKİ SARIKAYA

**Abstract.** We establish new perturbed Ostrowski type inequalities for functions whose second derivatives are of bounded variation. In addition, we obtain some integral inequalities for absolutely continuous mappings. Finally, some inequalities related to Lipschitzian derivatives are given.

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**Key words.** Function of bounded variation, perturbed Ostrowski type inequalities.

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*Bartın University*

*Department of Mathematics*

*Bartın, Turkey*

*E-mail: erdensmt@gmail.com*

<https://orcid.org/0000-0001-8430-7533>

*Düzce University*

*Department of Mathematics*

*Düzce, Turkey*

*E-mail: hsyn.budak@gmail.com*

<https://orcid.org/0000-0001-8843-955X>

*E-mail: sarikayamz@gmail.com*

<https://orcid.org/0000-0002-6165-9242>