

EXISTENCE OF SOLUTIONS FOR SOME DEGENERATE
SEMILINEAR ELLIPTIC EQUATIONS WITH MEASURE DATA

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Abstract. We study the existence of a weak solution for the degenerate semilinear elliptic problem

$$-\sum_{i,j=1}^n D_j(a_{ij}(x)D_i u(x)) - \lambda g(x)u(x) = -f(x, u(x)) + \mu \quad \text{in } \Omega$$

$$u = 0 \quad \text{on } \partial\Omega,$$

where Ω is a bounded open subset of \mathbb{R}^N , $N \geq 2$ and λ is a real parameter. Here $g : \Omega \rightarrow \mathbb{R}$ and $f : \Omega \times \mathbb{R} \rightarrow \mathbb{R}$ are functions satisfying suitable hypotheses and μ is a Radon measure.

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