

CYCLES OF REDUCED IDEALS AND CLASS NUMBER
OF PURE CUBIC NUMBER FIELD

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Abstract. For some pure cubic field K , we compute the class number of K based on the notion of reduced ideals and the notion of the minimum of an ideal.

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Key words. Cubic field, minimum of ideal, reduced ideal, cycle of reduced ideal.

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