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GENERALIZATIONS OF REGULAR AND NORMAL SPACES II

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Abstract. A family m_X of subsets of a nonempty set X is called an m-structure [17]. A set X with a topology τ and m-structure m_X is called a mixed-space and is denoted by (X, τ, m_X). As a generalization of g-closed sets due to Levine [10], we introduce the notion of m_g-closed sets in (X, τ, m_X). By using m_g-open sets, we define and investigate mixed-regularity and mixed-normality in (X, τ, m_X). As special cases, we obtain $\mathcal{I}_g$-regular spaces [13] and s-normal spaces [8].

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