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COEFFICIENT INEQUALITIES FOR CERTAIN CLASSES OF ANALYTIC FUNCTIONS USING q-DERIVATIVES

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Abstract. We introduce and we study the classes $\mathcal{ST}_q(g,\lambda,\gamma,\alpha,\beta)$ and $\mathcal{KV}_q(g,\lambda,\gamma,\alpha,\beta)$ of analytic functions which are defined by making use of the q-derivative operator. Coefficient inequalities for functions in these classes are discussed. Some interesting consequences of the results are also pointed out.

MSC 2010. 30C45; 30C50.

Key words. Analytic function, univalent function, starlike function, convex function, convolution, q-derivative operator.

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