

A SHORT NOTE ON HARMONIC FUNCTIONS ON
SELF-SIMILAR STRUCTURES

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Abstract. A sufficient condition is given concerning the harmonic structure on a post critically finite self-similar structure K that ensures that harmonic functions are not zero divisors in the algebra of real-valued continuous functions on K .

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Key words. Self-similar structure, harmonic function, Sierpinski fractal.

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