

POSITIVE SOLUTIONS FOR DISCRETE
ANISOTROPIC EQUATIONS

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Abstract. Using variational method, we study the existence of positive solutions for an anisotropic discrete Dirichlet problem with some functions α, β and a nonlinear term f .

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