

ON THE SUBCENTRAL AUTOMORPHISMS
OF FINITE GROUPS

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Abstract. Let G be a group and let M be a characteristic subgroup of G . We denote by $\text{Aut}_M^M(G)$ the set of all automorphisms of G which centralize G/M and M . In this paper, we give necessary and sufficient conditions for the equality of $\text{Aut}_M^M(G)$ with $\text{Aut}^M(G)$ and $C_{\text{Aut}_M^M(G)}(Z(G))$.

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