

## ON THE NON-COMMUTING GRAPH OF A GROUP

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**Abstract.** In this paper, groups whose non-commuting graphs are  $k$ -apex for  $1 \leq k \leq 5$  are classified. The 1-planarity of the non-commuting graph for an AC-group  $G$  is discussed. Moreover, the  $k$ -connectivity of the non-commuting graph is verified, for  $k \leq 6$ . Finally, some properties of the line graph of the non-commuting graph of a group are studied.

**MSC 2010.** Primary 05C25, 05C10, 05C76; Secondary 20B05.

**Key words.** Apex graph, connected graph, non-commuting graph.

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