MATHEMATICA, 61 (84), N° 1, 2019, pp. 183–189

SHEETS OF CONJUGACY CLASSES IN SIMPLE ALGEBRAIC GROUPS

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Abstract. For a connected reductive algebraic group G defined over an algebraically closed field of characteristic p the sheets of conjugacy classes have been parametrized by G. Carnovale and F. Esposito when p is good for G. We show that the method is independent of characteristic and that a similar parametrization is possible for all p.

MSC 2010. 14L10, 14L35, 14L40.

Key words. Algebraic groups, Jordan classes, sheets of conjugacy classes.

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DOI: 10.24193/mathcluj.2019.2.08

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Received June 24, 2018
Accepted August 3, 2018

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