

NEW INTEGRAL INEQUALITIES FOR (r, α) -FRACTIONAL
MOMENTS OF CONTINUOUS RANDOM VARIABLES

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Abstract. In this paper, we establish new integral inequalities for continuous random variables. By introducing new concepts on fractional moments of continuous random variables, we generalize some interesting results of P. Kumar. Other fractional integral results are also presented.

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Key words. Integral inequalities, Riemann-Liouville integral, random variable, fractional dispersion, fractional variance, fractional moment.

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