RINGS WHOSE UNITS COMMUTE
WITH NILPOTENT ELEMENTS

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Abstract. Rings with the property in the title are studied under the name of "uni" rings. These are compared with other known classes of rings and, since commutative rings and reduced rings trivially have this property, conditions which added to uni rings imply commutativity or reduceness are found.

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Key words. Uni ring, reduced ring, nilpotent-central ring, commuting nilpotents.

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