ESTIMATION OF INEXACT RECIPROCAL-QUINTIC AND RECIPROCAL-SEXTIC FUNCTIONAL EQUATIONS

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Abstract. The purpose of this study is to investigate Ulam stability of reciprocal-quintic and reciprocal-sextic functional equations in non-Archimedean fields pertinent to the results ascertained by Hyers, Rassias, and Găvruta. Illustrative examples are provided to show that the results are not valid for the singular cases.

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Key words. Hyers-Ulam stability, non-Archimedean field, reciprocal functional equation, reciprocal-quintic functional equation, reciprocal-sextic functional equation.

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