

DIFFERENTIABLE MAPS  
WITH UNCOUNTABLE CRITICAL SETS

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**Abstract.** In this paper we provide some sufficient conditions on two manifolds which ensure uncountable critical sets for all smooth maps between the two manifolds. These sufficient conditions are given in terms of Stiefel-Whitney classes of the two manifolds and their duals.

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