

SUR LE 3-RANG DU GROUPE DE CLASSES
DE CERTAINS CORPS QUADRATIQUES RÉELS

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Abstract. We determine a family of real quadratic fields whose 3-rank of class groups is greater than or equal to 2.

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