

ON \mathfrak{m} -IRREDUCIBILITY OF \mathcal{M} -SPACES

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Abstract. We introduce \mathfrak{m} -irreducible spaces and infratopological spaces. These notions generalize notions of topological space and irreducible space [T. Thompson, *Characterizations of irreducible spaces*, Kyungpook Math. J., **21**(2) (1981), 191–194]. Characterizations of \mathfrak{m} - T_2 spaces and characterizations of \mathfrak{m} -irreducible spaces are obtained. Our research leads to several generalizations of some well-known results.

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Key words. Infraspaces, supraspace, \mathfrak{m} -Hausdorff, \mathfrak{m} -irreducible, \mathfrak{m} - α -open, \mathfrak{m} -semi-open, \mathcal{M} -continuity.

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