

ON WEIGHTED MONTGOMERY IDENTITY
FOR RIEMANN-LIOUVILLE FRACTIONAL INTEGRALS

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Abstract. In this paper, we extend the weighted Montgomery identity for the Riemann-Liouville fractional integral. We also use this Montgomery identity to establish some new weighted Ostrowski type integral inequalities.

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