

AN ANALOG OF TITCHMARSH'S THEOREM
FOR THE DUNKL TRANSFORM IN THE SPACE $L^p(\mathbb{R}^d, w_k(x)dx)$

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Abstract. Using a generalized spherical mean operator, we obtain an analog of Titchmarsh's theorem for the Dunkl transform for functions satisfying the (β, k) -Dunkl Lipschitz condition in the space $L^p(\mathbb{R}^d, w_k(x)dx)$, where $1 < p \leq 2$ and w_k is a weight function, invariant under the action of an associated Weyl group.

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