AN INTERMEDIATE NEWTON-KANTOROVICH METHOD FOR SOLVING NONLINEAR EQUATIONS

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Abstract. We provide a semilocal convergence analysis for an easy to implement intermediate Newton-Kantorovich method in order to approximate a locally unique solution of a nonlinear equation in a Banach space setting.

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Key words. Newton-Kantorovich type methods, Banach space, majorizing sequence, nonlinear equation, Fréchet-derivative.

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