

AN IMPROVED LOCAL CONVERGENCE ANALYSIS FOR  
SECANT-LIKE METHOD

IOANNIS K. ARGYROS and SAÏD HILOUT

**Abstract.** We provide a local convergence analysis for Secant-like algorithm for solving nonsmooth variational inclusions in Banach spaces. An existence-convergence theorem and an improvement of the ratio of convergence of this algorithm are given under center-conditioned divided difference and Aubin's continuity concept. Our result compare favorably with related obtained in [18].

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**Key words.** Banach space, Secant-like method, generalized equation, Aubin continuity, ratio of convergence, divided difference, set-valued map.

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*Cameron University*  
*Department of Mathematical Sciences*  
*Lawton, OK 73505, USA*  
*E-mail: iargyros@cameron.edu*

*Poitiers University*  
*Laboratoire de Mathématiques et Applications*  
*Bd. Pierre et Marie Curie, Téléport 2, B.P. 30179*  
*86962 Futuroscope Chasseneuil Cedex, France*  
*E-mail: said.hilout@math.univ-poitiers.fr*