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LOEWNER CHAINS AND GENERALIZED ALMOST STARLIKE MAPPINGS

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Abstract. In this paper, we introduce the notion of generalized almost starlikeness on the unit disc as well as on the unit ball B^n in $\mathbb{C}^n$, and we prove that this notion can be characterized in terms of Loewner chains. Finally, we use the theory of Loewner chains to deduce that certain classes of generalized Roper-Suffridge extension operators preserve generalized almost starlikeness.

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Key words. Loewner chain, Roper-Suffridge extension operator, spirallike function, starlike function, subordination,subordination chain, biholomorphic mapping.

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