

SUBCLASSES OF STARLIKE FUNCTIONS
INVOLVING A CERTAIN INTEGRAL OPERATOR

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Abstract. Making use of the generalized integral operator, we define a new subclass of uniformly convex functions and a corresponding subclass of starlike functions with negative coefficients and obtain coefficient estimates, extreme points, the radii of close to convexity, starlikeness and convexity. In particular, we obtain integral means inequalities for the function $f(z)$ belongs to the class $UCT(\alpha, \beta, \gamma, \lambda, m)$ in the unit disc.

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