

ON BLOCKS AND CLIFFORD EXTENSIONS

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Abstract. We give a short proof of a result of E.C. Dade, as stated in [1, Theorem 9] on Clifford extensions for blocks of group algebras (see also [2, Corollary 12.6], avoiding the machinery developed in [2], but making use of the Brauer homomorphism. Moreover, we do not assume that the ground field k is algebraically closed.

MSC 2010. 20C20, 16S35, 20C05.

Key words. Group algebra, blocks, group graded algebra, Brauer homomorphism, Brauer correspondence.

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