ENTIRE UNBOUNDED FUNCTIONS ON BANACH SPACES WITH A MONOTONE SCHAUDER BASIS

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Abstract. It is well-known that on any complex infinite dimensional Banach space there is an entire function that is unbounded on some ball. Here we shall give an explicit construction of such entire functions on any infinite dimensional complex normed space with a monotone Schauder basis.

MSC 2010. 46G20.

Key words. Entire function, monotone Schauder basis.

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