

APPROXIMATION OF FUNCTIONS  
OF WEIGHTED LEBESGUE AND SMIRNOV SPACES

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**Abstract.** In this work we investigate the inverse approximation problems in the Lebesgue and Smirnov spaces with weights satisfying the so-called Muckenhoupt's  $A_p$  condition in terms of the  $\alpha$ -th mean modulus of smoothness,  $\alpha > 0$ . We obtain a converse theorem of trigonometric approximation in the weighted Lebesgue spaces and obtain some converse theorems of algebraic polynomial approximation in the weighted Smirnov spaces.

**MSC 2010.** Primary 30E10, 46E30; Secondary 41A10, 41A25, 41A27, 42A10.

**Key words.** Weighted Smirnov spaces, Dini-smooth curve, inverse theorems, fractional modulus of smoothness.

REFERENCES

- [1] HACIYEVA, E.A., *Investigations of the properties of functions with quasimonotone Fourier coefficients in generalized Nikolskii-Besov spaces*, Author's summary of Dissertation, Tbilisi, 1986 (in Russian).
- [2] ISRAFILOV, D.M. and AKGÜN, R., *Approximation in weighted Smirnov-Orlicz classes*, J. Math. Kyoto Univ., **46** (4) (2006), 755-770.
- [3] ISRAFILOV, D.M. and GUVEN, A., *Approximation in weighted Smirnov classes*, East J. Approx., **11** (1) (2005), 91-102.
- [4] KY, N.X., *Moduli of mean smoothness and approximation with  $A_p$ -weights*, Ann. Univ. Sci. Budapest. Sect. Math., **40** (1997), 37-48.
- [5] KY, N.X., *An Alexits's lemma and its applications in approximation theory*, Functions, Series, Operators (L. Leindler, F. Schipp, J. Szabados, eds.), Budapest (2002), 287-296.
- [6] TABERSKI, R., *Two indirect approximation theorems*, Demonstratio Math., **9** (2) (1976), 243-255.
- [7] TABERSKI, R., *Approximation of functions possessing derivatives of positive orders*, Ann. Polon. Math., **34** (1977), 13-23.
- [8] TABERSKI, R., *Differences, moduli and derivatives of fractional orders*, Comment. Math., **19** (1977), 389-400.
- [9] ZYGMUND, A., *Trigonometric series*, I and II, Cambridge University Press, 1959.

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