

REMARKS ON GENERALIZED BRAUER PAIRS

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Abstract. Let k be an algebraically closed field of characteristic p , G a finite group, N a normal subgroup of G and c a G -stable block of kN . Then there exist generalized Brauer pairs, called (c, G) -Brauer pairs, and denoted by (Q, e_Q) , where Q is a p -subgroup of G and e_Q a block of $kC_N(Q)$. If $G = N$, then the generalized Brauer pairs becomes the usual c -Brauer pairs. If (P, e_P) is a maximal (c, G) -Brauer pair, we prove that e_P is a nilpotent block. We also prove a generalization of Brauer's third main theorem.

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Key words. Finite group, block, generalized Brauer pair, Brauer homomorphism.

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