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MULTIPLE SOLUTIONS FOR A NON-HOMOGENEOUS NEUMANN BOUNDARY-VALUE PROBLEM

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Abstract. In this paper we obtain multiple solutions in double weighted Sobolev spaces for a non-homogeneous elliptic semilinear eigenvalue problem on unbounded domain. We use a very recent Ricceri type critical points theorem proved by Kristály, Marzantowicz, Varga in [4].

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