# HARMONIC FUNCTIONS WHICH ARE STARLIKE OF COMPLEX ORDER WITH RESPECT TO CONJUGATE POINTS

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**Abstract.** Let $H$ denote the class of functions $f$ which are harmonic, orientation preserving and univalent in the open unit disc $D = \{z : |z| < 1\}$. This paper defines and investigates a family of complex-valued harmonic functions that are orientation preserving and univalent in $D$ and are related to the functions starlike of complex order with respect to conjugate points. The authors obtain coefficient conditions and growth result.

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**Key words.** Harmonic functions, starlike of complex order, coefficient estimates.

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