

## IMPROVED RESULTS FOR CONTINUOUS MODIFIED NEWTON-TYPE METHODS

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**Abstract.** We provide semilocal convergence results for continuous modified Newton-type methods to solve nonlinear operator equations in a real Hilbert space setting. Using a combination of Lipschitz and center Lipschitz continuous conditions, we provide a finer convergence analysis than before under weaker conditions, and the same hypotheses and computational cost [1]-[4], [11]-[15]. In this way we expand the applicability of Newton-type continuous methods under the same computational cost as before.

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**Key words.** Hilbert space, Banach space, Fréchet-derivative, continuous Newton-type methods.

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