

LOEWNER CHAINS AND QUASICONFORMAL EXTENSIONS OF  
HOLOMORPHIC MAPPINGS IN  $\mathbb{C}^n$

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**Abstract.** In this paper, by using the method of Loewner chains, we give an univalence criterion which contains as particular cases some univalence criteria for holomorphic mappings in the unit ball of  $\mathbb{C}^n$ . Also, we obtain a sufficient condition for a normalized quasiregular mapping  $f \in \mathcal{H}(B)$  to be extended to a quasiconformal homeomorphism of  $\mathbb{R}^{2n}$  onto itself.

**MSC 2000.** 32H99, 30C45.

**Key words.** Loewner chains, Loewner differential equation, quasiregular mapping, quasiconformal mapping, quasiconformal extension.

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