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## EPIC ENVELOPES BY GENERALIZED FLAT MODULES

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**Abstract.** We establish equivalent conditions under which every right R-module has an epic  $\mathcal{X}$ -envelope, when  $\mathcal{X}$  is a Tor-orthogonal class of left-R-modules. As particular cases, one may recover and complete known results on various generalizations of flatness.

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Key words. Envelope, flat module.

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