

A NOTE ON FLAT COVERS OF COMODULES

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Abstract. We present another proof for the existence of a flat cover for every comodule over a semiperfect coalgebra.

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Key words. Flat cover, comodule, semiperfect coalgebra.

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