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ON NEIGHBORHOODS OF CERTAIN CLASSES OF ANALYTIC FUNCTIONS WITH NEGATIVE COEFFICIENTS

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Abstract. Let $\mathcal{A}(n)$ denote the class of functions of the form

$$f(z) = z - \sum_{k=n+1}^{\infty} a_k z^k, \quad (a_k \geq 0,\ n \in \mathbb{N} = \{1, 2, \dots\}),$$

which are analytic in the open unit disk $\mathcal{U} = \{z : |z| < 1\}$. In this note, we define certain subclasses $\mathcal{S}_n^*(A, B)$, $\mathcal{C}_n(A, B)$, $\mathcal{R}_n(A, B)$, $\mathcal{Q}_n(A, B)$, $\mathcal{S}_n(A, B; C, D)$ and $\mathcal{C}_n(A, B; C, D)$ of $\mathcal{A}(n)$ and some properties of neighborhoods are studied for these classes.

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