

CHARACTERIZATIONS OF CLOSED SETS IN PRODUCT SPACES

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Abstract. In this paper we characterize different types of closed sets in product spaces using the notion of upper limit.

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