

INVARIANTS OF INFINITE BLASCHKE PRODUCTS

TUAN CAO-HUU and DORIN GHISA

Dedicated to Professor Petru T. Mocanu

Abstract. The analytic continuation by symmetry with respect to the unit circle of infinite Blaschke products is studied and invariants of the restriction to some parts of the unit circle of these extended functions are obtained. Then analytic extensions of the respective invariants are constructed. The analogous results for infinite Blaschke products on the real projective plane are stated.

MSC 2000. 34C40.

Key words. Infinite Blaschke products, symmetry principle, groups of invariants, real projective plane.

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Received September 17, 2006

*York University – Glendon campus
Department of Computer Science and Mathematics
2275 Bayview Avenue
Toronto, Ontario
Canada M4N 3M6
E-mail: tuan@nmr.mgh.harvard.edu
E-mail: dghisa@yorku.ca*