

## TOTALLY REFLEXIVE, TOTALLY SYMMETRIC PATTERN ALGEBRAS

ENDRE VÁRMONOSTORY

**Abstract.** A  $k$ -ary relation  $\rho$  on a set  $A$  induces a partition of each power  $A^n$  into “patterns” in a natural way. An operation on  $A$  is called a  $\rho$ -pattern operation if its restriction to each pattern is a projection. We examine functional completeness of algebras with  $\rho$ -pattern fundamental operations in the case when  $\rho$  is the totally reflexive, totally symmetric relation of  $A$ .

**MSC 2000.** 08A40.

**Key words.** Majority function, semiprojection, central relation, minimal central relation, functionally completeness.

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*University of Szeged*  
*Faculty of Juhász Gyula*  
*Teacher's Training College*  
*Boldogasszony sgt. 6.sz.*  
*6725 Szeged, Hungary*  
*E-mail: varmono@jgytf.u-szeged.hu*