

(CO)TRIPLES AND HOCHSCHILD (CO)HOMOLOGY OF
SUPERALGEBRAS

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Abstract. We show that the Hochschild homology and cohomology of a given (not necessarily commutative) \mathbb{Z}_2 -graded algebra (superalgebra) R over a graded-commutative \mathbb{Z}_2 -graded ring, with coefficients in an R -bimodule can be defined as the homology (cohomology) of a suitable chosen cotriple (triple), with coefficients in a functor.

MSC 2000. 17A70, 16E40, 18C15

Key words. Superalgebras, Hochschild homology, triples.

Acknowledgment. This paper was partially supported by the European Commission, through the Research Training Network “Geometric Analysis”.

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Received November 15, 2004

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