

SOME REMARKS ON DIFFERENTIAL INCLUSIONS
WITH STATE CONSTRAINTS

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Abstract. We prove the existence of solutions to lipschitzean integrodifferential inclusions viable in a closed set contained in R^n . Using this result we study the infinitesimal properties of functions which are nonincreasing along all the trajectories of a differential inclusion.

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Key words. Lipschitzean set-valued maps, differential inclusions, viable solutions, generalized derivatives.

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