ON THE NUMBER OF CONJUGACY CLASSES OF FINITE p-GROUPS

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Abstract. Denote by k(G) the number of conjugacy classes of a group G. Some inequalities are deduced by arithmetic means for k(G), where G is a p-group. As an application, k(G) is calculated for special cases of p-groups. A method of estimating k(G) for some finite groups, others then p-groups is also presented.

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