

LOCAL EXISTENCE OF SOLUTIONS TO A CLASS
OF NONCONVEX SECOND ORDER
DIFFERENTIAL INCLUSIONS

AURELIAN CERNEA

Abstract. We prove the local existence of solutions to the Cauchy problem $x'' \in F(x, x') + f(t, x, x')$, $x(0) = x_0, x'(0) = y_0$, where F is a set-valued map contained in the Fréchet subdifferential of a ϕ -convex function of order two and f is a Carathéodory single valued map.

MSC 2000. 34A60.

Key words. Differential inclusions, lower regular function, Clarke subdifferential.

REFERENCES

- [1] ANCONA, F. and COLOMBO, G., *Existence of solutions for a class of nonconvex differential inclusions*, Rend. Sem. Mat. Univ. Padova., **83** (1990), 71–76.
- [2] AUBIN, J.P. and CELLINA, A., *Differential Inclusions*, Springer, Berlin, 1984.
- [3] BRÉZIS, H., *Opérateurs maximaux monotones et semi-groupes de contractions dans les espaces de Hilbert*, North-Holland, Amsterdam, 1973.
- [4] BRÉZIS, H., *Analyse fonctionnelle, théorie et applications*, Masson, Paris, 1983.
- [5] CARDINALI, T., COLOMBO, G., PAPALINI, F. and TOSQUES, M., *On a class of evolution equations without convexity*, Nonlinear Anal., **28** (1996), 217–234.
- [6] CERNEA, A., *On the local existence of solutions to a class of second order differential inclusions*, An. Univ. Buc., to appear.
- [7] CERNEA, A., *On a nonconvex second order differential inclusion*, Bull. Math. Soc. Sci. Math. Roum., to appear.
- [8] CORNET, B. and HADDAD, B., *Théoreme de viabilité pour inclusions différentielles du second order*, Israel J. Math., **57** (1987), 225–238.
- [9] DEGIOVANNI, M., MARINO, A. and TOSQUES, M., *Evolution equations with lack of convexity*, Nonlinear Anal., **9** (1995), 1401–1443.
- [10] HA, T. D. X. and MARQUES, M., *Nonconvex second order differential inclusions with memory*, Set-valued Anal., **5** (1995), 71–86.
- [11] LUPULESCU, V., *Existence of solutions to a class of second order differential inclusions*, Cadernos de Matematica, Aveiro Univ. CM01/I-11.
- [12] MARCO, L. and MURILLO, J.A., *Viability theorems for higher-order differential inclusions*, Set-valued Anal., **6** (1998), 21–37.

Received October 22, 2002

*Faculty of Mathematics and Informatics
University of Bucharest
Str. Academiei 14
RO-010014 Bucharest, Romania
E-mail: acernea@math.math.unibuc.ro*