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Logarithmic Sobolev inequalities on Euclidean submanifolds: sharpness, rigidity and applications

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Abstract

We provide Michael–Simon-type L^p -logarithmic-Sobolev inequalities on complete, not necessarily compact *n*-dimensional submanifolds Σ of the Euclidean space \mathbb{R}^{n+m} . Our estimate is sharp, and it involves the mean curvature of Σ . Equality can only occur if and only if Σ is isometric to the Euclidean space \mathbb{R}^n and the extremizer is a Gaussian. Applications are provided to sharp hypercontractivity estimates of Hopf–Lax semigroups on submanifolds. This is a joint work with Alexandru Kristály.