

GENERALIZATIONS OF EDELSTEIN'S FIXED POINT THEOREM IN COMPACT METRIC SPACES

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Abstract. We study deeply some fixed point theorem in compact metric spaces proved very recently, generalizing this theorem. We also show this theorem is a generalization of the famous Edelstein's fixed point theorem.

Key Words and Phrases: Nonspreading mapping, condition (CC), fixed point, convergence theorem, quasimetric space, Edelstein's fixed point theorem.

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