FIXED POINT ALGORITHMS
FOR SPLIT FEASIBILITY PROBLEMS

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Abstract. The purpose of the paper is to investigate a split feasibility problem based on a fixed point algorithm. A weak convergence theorem of solutions is established in the framework of infinite dimensional Hilbert spaces. As an application, a split equality problem is also investigated.

Key Words and Phrases: Hilbert space, monotone mapping, nonexpansive mapping, split feasibility problem, weak convergence.

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